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THESIS

FOR THE

Degree of Bachelor of Science

IN

MINE ENGINEERING.



SUBJECT,

"Furnace Calculations."

7525

JNO. M. BROOKS, JR.

JUNE, 1906.

FURNACE CALCULATIONS.

-----000-----

PROBLEM.

A furnace that will smelt a given amount of material per twenty-four hours, to dimension parts, and finally draw the complete plans. Copper Matting Furnace.

- (1) Smelt say ninety tons in twenty-four hours.
Should smelt this in, say, four charges per twenty-four hours. Of this take four and one-half hours to smelt each charge, and one and one-half hours to skim and charge, and fix up bed of fuel.
- (2) Fuel to be bituminous coal, direct fired.

Ash	15 %
Flx C.	44.5 %
Vol Matter	40 %

Heat about 8,000 calories = 8,000 pound calories.
- (3) In ordinary practice in work similar to this, they use 3.5 tons of charge per one ton of coal. Compute the theoretical amount of heat generated by such coal as is used, then the actual amount of heat required to

bring material to a slag and matte at, say, 1000° C. by reactions. This will involve classifying your slag, figuring formation heats of silicates, reduction of Fe_2O_3 to FeO , etc., for the various reactions.

From this get an idea of coal efficiency. This efficiency will then serve as a guide in your own calculations.

Slag made was:

34.5 % SiO_2
43. % FeO (MnO)
8.5 % Al_2O_3
14.0 % ZnO
0.6 % Cu
1.0 oz Ag
3.56 = Spgr

Matte made was:

50.0 % Cu
4.8 = Spgr
100 ozs Ag.

This matte is 8% higher than the actual per cent S. in the roasted ore would theoretically call for.

Common practice in smelting, in burning fuel, shows about twice as much air drawn through the grate as is theoretically required to burn the coal.

Calculate this amount with coal consumption, calculate the total heat generated at the rate of combustion of your coal, and the pyrometric effect as nearly as possible. Will have to assume that the products of combustion

Design furnace, using fire and red brick in the proper places.

Ref. (See Ingell's Heating and Furnace Design.)

Classification of Slag:

$2\text{Al}_2\text{O}_3 \cdot 3\text{SiO}_2$ = mono-silicate of aluminum.

$$\frac{2\text{Al}_2\text{O}_3}{3\text{SiO}_2} = \frac{8.5}{X} = \frac{(27 \times 2 + 16 \times 3)2}{3 \times 60} = \frac{204}{180}$$

$X = 7.5\# \text{SiO}_2$ required to form mono-silicate of aluminum.

Slag Analysis:

34.5 % SiO_2

43.0 % FeO

8.5 % Al_2O_3

14.0 % ZnO

0.6 % Cu

1.0 oz Ag

3.56 = Spgr

$2 \text{ZnO} \cdot \text{SiO}_2$ = Mono-silicate.

$$\frac{2\text{ZnO}}{\text{SiO}_2} = \frac{14}{X} = \frac{162.8}{60}$$

$$162.8X = 840$$

$X = 5.16\# \text{SiO}_2$ required to form $2\text{ZnO} \cdot \text{SiO}_2$.

with the 14# ZnO in slag.

7.5
5.16
12.66# SiO_2 required for Al_2O_3 and ZnO

34.50# SiO_2 = total in slag per 100#

21.84# SiO_2 remains, therefore to combine with iron.

2 FeO . SiO₂ = mono-silicate of iron

FeO . SiO₂ = bi-silicate of iron

2 FeO . 3SiO₂ = sesqui-silicate of iron

2 FeO . SiO₂ = proto- or sub-silicate of iron.

$$\frac{2 \cdot \text{FeO}}{\text{SiO}_2} = \frac{144}{60} = \frac{43}{X}$$

$$144X = 2580$$

X = 18 Kgm SiO₂ required for 43 Kgm FeO as mono-silicate.

For bi-silicate would have:

$$\frac{\text{FeO}}{\text{SiO}_2} = \frac{43}{X} = \frac{72}{60}$$

$$X = 35.8 \text{ Kgm SiO}_2 \text{ to form bi-silicate.}$$

Sesqui-silicate would require 26.9 Kgm SiO₂. Have only 21.9 Kgm SiO₂, so approximates more closely the mono-silicate than any other, but lays between the mono- and sesqui-silicates.

If, therefore, 10 Kgm FeO goes to form the bi-silicate, and the other 33 Kgms remaining goes to form a mono-silicate, there will be required 22.0 Kgm SiO₂. Assuming then, that a certain amount of the FeO and SiO₂ have combined to form the bi-silicate, and the rest forms a mono-silicate in which the bi-silicate remains

in solution, analagous to CO and CO_2 in furnace gases, or SO_2 and SO_3 in roaster gases, we have the following disposition of material:

Al_2O_3	9.5 Kgm;	SiO_2	7.5 Kgm Mono-silicate
ZnO	14.0 Kgm;	SiO_2	5.16 Kgm Mono-silicate
$\text{FeO}43$	33.0 Kgm;	SiO_2	13.7 Kgm Mono-silicate
$\text{FeO}43$	10.0 Kgm;	SiO_2	2.3 Kgm Bi-silicate

34.66

34.5 Kgm SiO_2 present

.16 Kgm SiO_2 more than

actually have, or 23.2% FeO forms bi-silicate, and 76.8% FeO goes to form mono-silicate.

537# FeO forms bi-silicate = 230. Kgm

1743# FeO forms singulo-silicate = 700.6 Kgm.

Size of Grate in Problem:

Ninety tons in forty charges, or two hundred and twenty-five tons per charge requires about one ton of coal per thirty-five tons of charge, so $\frac{22.5}{35} = 6.43$ tons of coal per charge. Four charges per twenty-four hours regular running, or $\frac{6.43}{6} = 1.07$ tons of coal per hour = 2140# per hour. Allowing 20# per square foot per hour grate area = 107 ' or grate is 8'-0" X 13'-5"

According to Bent, 10# per square foot per hour gives the most efficient results, and as high temperature

can be obtained, common practice runs much higher, however, and 40# is not an uncommon figure in boiler practice.

This is entirely too rapid combustion for the reverberatory furnace, and in fact an entirely different result is the object.

In reverberatory practice a long flame is desired, and but little actual burning in the grate. The flame and products of combustion and distillation of the coal, pass over the fire bed in a rather cramped condition, and develop in the laboratory of the furnace, and it is there that complete combustion takes place, and the intense heat of the flame develops.

In order ~~xxx~~ to accomplish this, and obtain a long flame, it is necessary to use an extremely thick bed of fuel, and to have only partial combustion taking place in the fire box. In fact the length of the flame is directly proportioned to the thickness of the bed of fuel. For this reason the grate area is diminished to 5'-0" X 8'-0", and a thicker bed of fuel is used.

In gas with no visible smoke, and what is considered good and complete burning, have 2.5% CO.

Each Kgm carbon requires 2.66 Kgm O to burn to CO₂.

2.

Each Kgm carbon requires 1.33 Kgm O to burn to CO.

Each Kgm H requires 8 Kgm O to burn to H₂O.

The coal used in firing this furnace has approximately the following analysis:

Coal Analysis:

Mais	3.90%
H ₂ O (Comb)	12.56%
Fix Carbon	44.50%
H	4.50%
C	19.60%
Ash	13.50% plus 15% of the above

Fix Carbon, which goes into ash, so available carbon is 43.00%, while total ash is 15%.

Ash Analysis:

		corrected for 10% carbon
SiO ₂	44.15%	39.66
Fe ₂ O ₃	16.60	14.90
Al ₂ O ₃	37.90	34.14
CaO	1.00	0.90
MgO	0.40	0.36
S	2.04	.04
	100.00	Carbon 10.00

and this gives, per one hundred pounds of coal consumed, the following weights of substances going

9.

into ash, and carrying heat from the furnace:

Material in ash per one hundred pounds of coal
consumed:

SiO_2	8.08#
Fe_2O_3	0.55
Al_2O_3	5.10
CaO	.14
MgO	.05
S	.01
Carbon	<u>1.50</u>
	15.00

Matte = 50% Cu, and is 9% higher than the outcome expected. (See condition of problem)

The raw ore is concentrates carrying

15% Cu

10% SiO_2

The best recovery obtainable is about 93% Cu, and 5% is rational figure for slag loss.

Have a concentration then of

$$\frac{50}{15 - \text{loss in slag}} = \frac{50}{15 - (.05 \times 15)} = 3.64 \text{ cons.}$$

That is to say, 3.64 tons of raw material are put into one ton of matte, or the values, etc., from that amount of raw ore.

Calculating back, then we have in raw ore from the matte

$$1000 - (6 \times 8) + 31.7\# = 993.7\# \text{ Cu.}$$

31.7# comes from 2.64 tons .006 equal total Cu in raw ore.

This Cu will require sulphur to the extent of

$$\frac{\text{Cu}}{\text{S}} = \frac{12.66}{32} = \frac{952}{5} \quad \text{S} = 240\#$$

The rest of the matte will be made up of iron and sulphur. That is to say,

$$\frac{952}{50} = 1904\# \text{ matte}$$

$$952 = \text{Cu}$$

$$\frac{240}{1192} = \text{S}$$

$$1904 - 1192 = 712 \# \text{ FeS in matte}$$

$$\text{FeS} = \frac{56}{88} = 63.63\% \text{ Fe}$$

So $712 \times 63.63 = 453 \# \text{ Fe}$ and leaves $712 - 453 = 259 \# \text{ S}$ in matte. Also $40.3 \# \text{ S}$ more than calculated upon is volatilized so we get $50\% \text{ matte}$ rather than $42\% \text{ matte}$.

Now this Fe will be in original ore as Fe_2O_3 and equal $\frac{112 + 48}{112} \times 453 = 647.1 \# \text{ Fe}_2\text{O}_3$

From the slag we have the following

$$\text{ZnO} = 14\% \times 2.64 \times 2000 = 739.2 \#$$

$$\text{Al}_2\text{O}_3 = 8.5\% = 160.0 \#$$

$$\text{SiO}_2 = 10\% \text{ in con.} = 539.0 \#$$

$$= 24.5\% \text{ from fettling} = 1293.6 \#$$

$$\text{FeO} = 45\% = 2270.4 \# = \frac{72}{160} \text{ Fe}_2\text{O}_3 \text{ to } 2454.5 \#$$

all of which give a total weight of $7346.4 \#$ for the original charge.

Original Charge:

Cu	953.7#	953.7#	} from matte
S for Cu	240#		
S for Fe	259#		
Volatilized	40.3#	539.3#	
Fe ₂ O ₃ from 453# Fe		647.1#	

Fe_2O_3	from 2270.4#	$\text{FeO} = 2454.5\#$)	
ZnO	unchanged	$= 732.2\#$)	
Al_2O_3	"	$= 160.0\#$)	From slag
SiO_2	"	$= 522.0\#$)	

SiO_2 from furnace fettling = 1223.6# From 24.5% not
 accounted for
7346.4# in original ore.

Cu	203.7 X .4536	=	446.3 kilograms
	453.		
Fe	1704. X .4536	=	1005.6 "
S	400.0 X .4536	=	205.0 "
Zn	593. X .4536	=	269.0 "
Al	24.7 X .4536	=	32.4 "
	850.2		
Si	806. X .4536	=	385.7 "
O	271.0 X .4536	=	770.4 "

Combustion of the Coal:

1 Kilogram of coal in furring gives the following:

.43 Kgm Fix Carbon and

.196 Kgm Vol Carbon

.626 Kgm Carbon

So $.626 \times \frac{87000}{12} = 5071$ calories CO_2 .045 Kgm H_2O

$.045 \times \frac{68000}{2} = \frac{1553}{6034}$ calories H_2O total
calories

Now, in burning twelve kilograms of carbon, combine with thrity-two kilograms of oxygen to form 22.22 cubic meters of CO_2 , and for each kilogram C, 2.67 kilograms O, are required, so have:

$.626 \times 2.67 = 1.67$ Kgm O for the C, and for H have:

$.045 \times 8 = .360$ Kgm O, for the hydrogen

Total 2.03 Kgm O actually required.

Now it is good practice and ordinary, to use about 25% excess O in reverberatory, while in steam boiler practice, and other places where a thin bed of fuel is used, 100% excess is used. In this case, however, can keep it down to 25%. This gives total oxygen of $2.03 \times 1.25 = 2.54$ Kgm O.

Volume of Gases and temperature:

$$32 \text{ Kgm O} = 22.32 \text{ M}^3. \text{ So}$$

$$\text{O.} \quad \frac{254}{32} \times 22.32 = 1.76 \text{ cubic meters of O.}$$

$$\text{Air.} \quad \text{and } \frac{1.76}{20.8} \times 100 = 8.46 \text{ cubic meters of air; air being } 20.8 \% \text{ oxygen.}$$

$$\text{N.} \quad 8.46 - 1.76 = 6.70 \text{ cubic meters nitrogen}$$

For CO_2 have:

$$\text{CO}_2 \quad \frac{1.68 + .626}{44} \times 22.32 = 1.165$$

$$\text{Free O.} \quad 1.76 - 1.16 = .60 \text{ cubic meters of O.}$$

$$\text{H}_2\text{O have } (.045 \times 9 + .032 + .126) \times \frac{22.32}{18} = .7033$$

$$\text{Then } 6624 = (0.303 \text{ t} + .000027 \text{ t}^2) (6.70 + .60) +$$

$$+ (0.37 \text{ t} + .00022 \text{ t}^2) (1.165) +$$

$$+ (0.34 \text{ t} + .00015 \text{ t}^2) (.7033) +$$

$$6624 = \begin{cases} (2.2119 \text{ t} + .0001371 \text{ t}^2) \\ (0.4311 \text{ t} + .0002563 \text{ t}^2) \\ (0.2391 \text{ t} + .0001055 \text{ t}^2) \end{cases}$$

$$6624 = 2.8821 \text{ t} + .0005589 \text{ t}^2$$

$$11851851.85 = 5157. \text{ t} + \text{t}^2$$

$$\text{t}^2 + 5157 \text{ t} + (2578)^2 = 11851851.85 + (2578)^2$$

$$t = - 2578 \pm \sqrt{11351351.35 + 6646000}$$

$$t = - 2578 + 4300.9 = 1723^{\circ} \text{ C.}$$

Burn 2140# coal per hour =

2140X.4536 = 971. Kilograms per hour, or

16.2 Kilograms coal per minute.

Now, in ~~examining~~ burning one kilogram of coal have:

6.700 cubic meters N_2

0.600 " " O_2

1.165 " " CO_2

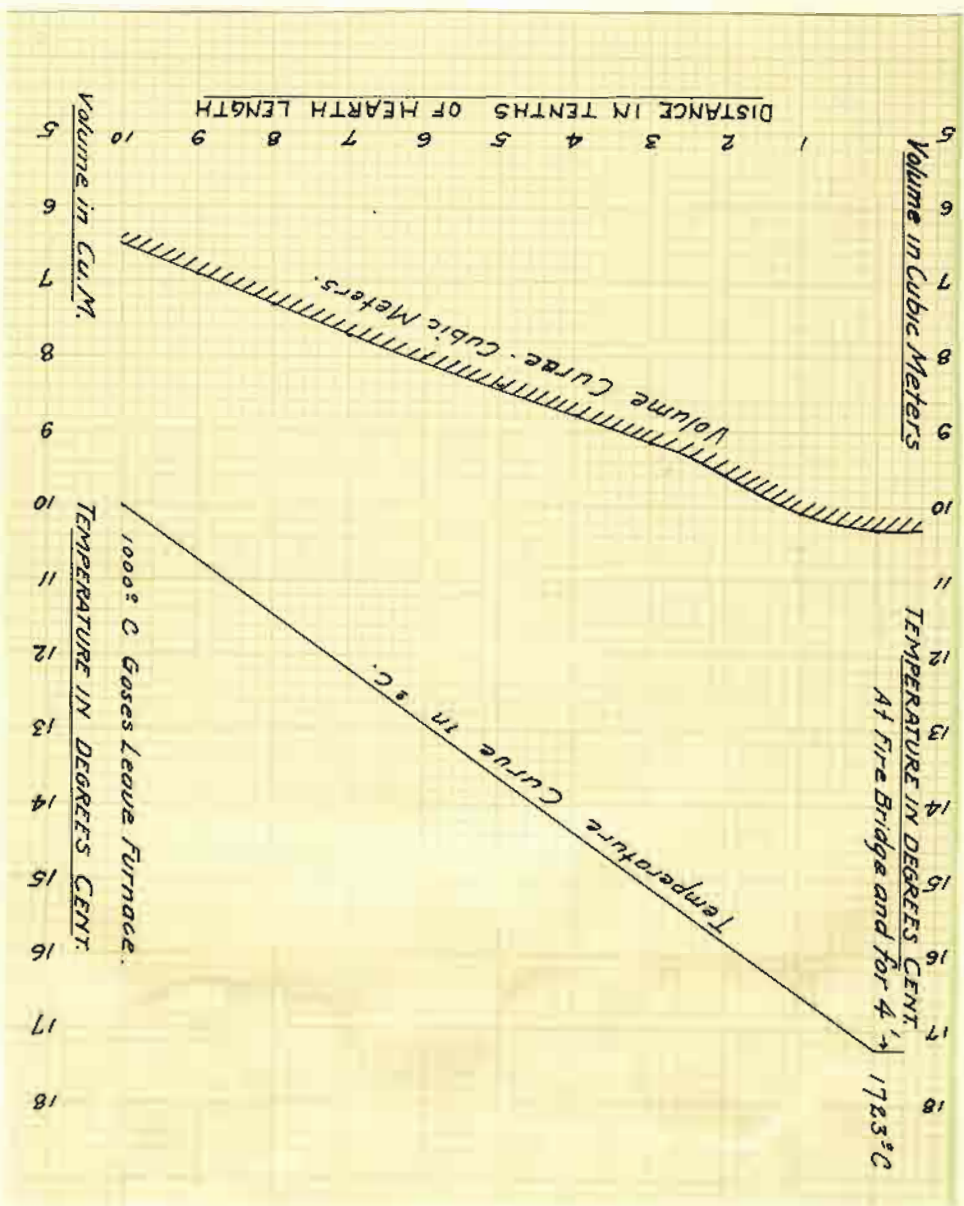
0.703 " " H_2O

9.168 " " Gas, or for 16.2 kilo-

grams have $16.2 \times 9.168 = 148.52$ cubic meters of gas at ordinary temperature, passing through furnace per minute.

Below is temperature curve and volume curve for furnace, beginning four feet from fire bridge.

(See next page)



Sp gr of gases: (Air = 1)

$$6.7 \text{ H}_2 \times .971 = 6.5057$$

$$0.6 \text{ O}_2 \times 1.105 = .6630$$

$$1.165 \text{ CO}_2 \times 1.529 = 1.7813$$

$$9.703 \text{ H}_2\text{O} \times 0.992 = .9674$$

$$9.168 \quad 9.6474 \quad | \quad 9.168$$

$$9.168 \quad | \quad 1.052 = \text{Density}$$

47940 of gases with

45340 air = 1

21000

$$h_o = 23 \left\{ \frac{1 - 1.052 + \frac{1}{273} \left(\frac{1000 + 400}{2} \right) - 1.052 \times 15}{\left(\frac{1 + \frac{1}{273} \times 15 \right) \left(\frac{1 + \frac{1}{273} \times \frac{1000 + 400}{2}} \right)} \right\}$$

$h_o = 15.019$ meters from

$$h = H \left\{ \frac{1 - \frac{1}{273} (t - Dt')}{\left(1 + \frac{1}{273} t' \right) \left(1 + \frac{1}{273} t \right)} \right\}$$

In which

H = Height of chimney in meters = 23

D = Sp gr of gases (air = 1) = 1.052

t = temperature in chimney = $\frac{1000 + 400}{2} = 700^\circ \text{C}$.

t' = temperature of outside air = 15°C .

h = total head in meters of air of 0°C .

Now the gases have velocity of three meters per second

(good practice), and the head required to give this is $h = \frac{3^2}{196} = .46$ m in terms of hot gas (700°C), or in terms of gas at 0°C $= 0.46 \times \frac{273}{400 + 273} = 1.06$ meters. For a velocity of three meters per second a diameter, d , will be required of

$$3 = \frac{\frac{148.52}{360}}{\frac{\pi d^2}{4}} = \frac{4 \times 7 \times 2.475}{32d^5} = 1.05 \text{ m}$$

$$d = \sqrt[5]{1.05} = 1.02 \text{ meters in diam.} = 3.3 \text{ ft.}$$

$$\text{Lost head due to friction} = h = .196 \times \frac{23}{1.02} \times .08$$

$$h \text{ friction} = 0.34 \text{ meters}$$

Which gives an effective head of $15.02 - (.19 + .34) = 14.5$ meters $= 44.03$ ft.

$44.03 \text{ ft air} = .0571 \text{ ft water} = .025\# = 0.6352 \text{ inches of water.}$

Total Volume of Cases:

$$\text{At fire bridge or 4' from same} = 148.52 \times \frac{1723+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 1027.$$

$$\text{At 1/10th point} = 148.52 \times \frac{1650+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 1013.$$

$$\text{at 2/10th point} = 148.52 \times \frac{1580+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 953.$$

$$\text{At 3/10th point} = 148.52 \times \frac{1510+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 917.$$

$$\text{At 4/10th point} = 148.52 \times \frac{1435+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 879.$$

$$\text{At 5/10th point} = 148.52 \times \frac{1360+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 840.$$

$$\text{At 6/10th point} = 148.52 \times \frac{1290+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 804.$$

$$\text{At 7/10th point} = 148.52 \times \frac{1220+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 768.$$

$$\text{At 8/10th point} = 148.52 \times \frac{1145+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 727.$$

$$\text{At 9/10th point} = 148.52 \times \frac{1075+273}{273} \times \frac{273}{273+15} \times \frac{14.7 - .025}{14.7} = 693.$$

$$\text{At exit point} = 145.52 \times \frac{1000 + 273}{273} \times \frac{273}{273 + 15} \times \frac{14.7}{14.7} = 0.55.0$$

Taking volume of exit point, and calculating from this the volumes at other points in per cent, we have inverse percentage curve shown in diagram on previous page. Also taking the volume at fire bridge, and calculating the relative volumes at different stages throughout furnace, we have the percentage curve shown in diagram.

Heat Required:

Fe_2O_3 to FeO

$$2454.5\# \times .4536 = 1112.36 \text{ kgm } \text{Fe}_2\text{O}_3$$

$$1112.36$$

$$(125600 - 265700) \frac{112}{112} = -237604.75 \text{ calories}$$

O_2

Fe_2O_3 to Fe

$$453\# \times 0.4536 = 205.4 \text{ kgm } \text{Fe}_2\text{O}_3$$

$$125600 \quad -352716.4$$

$$205.4 \times \frac{112}{112} =$$

$$-226521.15 \text{ calories}$$

Sources of Heat:

$$1 \quad 40.3\# \text{ O} \times .4536 = 18.28 \text{ calories}$$

$$69,200$$

$$18.28 \times \frac{112}{112} =$$

$$32$$

$$+32470.20 \text{ calories}$$

$$\text{FeO}_2(\text{SiO}_2) \quad 2270\# \text{ FeO} = 1020.7 \text{ kgm } \text{FeO}$$

Of this 232.9 kgm goes to form a bi-silicate, while the remaining 780.8 kgm go to form a singulo-silicate. There-

fore

$$\begin{array}{rcl}
 232.9 \times \frac{(254,000 - (65700 + 180000))}{56} & = & 37946.25 \text{ calories} \\
 \text{and } 790.9 \times \frac{(320400 - (2 \times 65700 + 180000))}{112} & = & 63562.50 \text{ " } \\
 \hline
 \text{Total heat} & & 140937.0 \text{ Calories}
 \end{array}$$

So $996321.15 - 140937.0$ calories = heat required to be
furnished by burning coal = 855384.15 calories

$$\begin{array}{rcl}
 \text{plus heat from following} & = & 729956.00 \text{ " } \\
 \hline
 & & 1585340.75
 \end{array}$$

$$1223.7\# \text{ Cu}_2\text{S} = 555.1 \text{ Kgm}$$

Besides the heat required for the reduction
of Fe_2O_3 and to FeO and Fe , there will be required
heat to melt down the charge and maintain it in
molten condition to cause the necessary reactions to
take place, or to make them possible, etc. These
amounts are estimated below:

Cu_2S
2

$$\begin{array}{rcl}
 \text{Heat in 1 Kgm Cu}_2\text{S at temperature of furnace } 1000^\circ & & \\
 \text{is} & - & 200.6 \text{ calories} \\
 \text{Heat in 1 Kgm Cu}_2\text{S at } 15^\circ\text{C} & & 1.7 \text{ " } \\
 \text{Heat required to bring 1 Kgm Cu}_2\text{S to } 1000^\circ & & 200.6 \text{ " }
 \end{array}$$

Latent heat of fusion, by 2.1 T Rule 14.3 calories
 Total heat to bring 1 Kgm of Cu_2S to 1000°C = 215.2 "
 Heat required for 555.1 Kgm = 119457.5 "

FeS.

Heat in 1 Kgm FeS at 1000°C =
 $1000 (.1357 + .000025 \times 1000) 1.0 = 135.7$ calories
 Heat in 1 Kgm 15°C is
 $15 (.1357 + .000025 \times 15) 1.0 = 2.04$ "
 Heat required to bring 1 Kgm FeS to 1000°C =
 133.66 "
 Latent heat of fusion =
 $\frac{2.1 (800 + 275)}{56 + 32} = 25.61$ "
 Heat 1 kgm = 159.27 "
 Total heat required to bring 712# FeS
 to 1000°C = $712 \times .4536 = 322.96$ Kgm
 $323 \times 184.2 = 59528.6$ calories

Mono-silicate of Iron $(\text{FeO})_2(\text{SiO}_2)$
 2

Heat required to bring 1 Kgm to 1000°C = 310 calories
 (See Vogt and Richards)
 Heat in 1 Kgm at 15°C = $15 (.1700 + .00004 \times 15) = 2.6$ "
 307.4 "
 Latent heat of fusion (Vogt) = 25.0 "
 Total heat per Kgm at 1000°C = 332.4 "

Total heat for 790.6 Kgm = $392.4 \times 790.6 = 310831.4$ calories

Si-silicates:

Heat required to bring 1 Kgm to 1000°C =

$$1000(.1646 + .00039 \times 1000)1.0 = 554.6 \text{ calories}$$

$$\text{Heat 1 Kgm at } 15^{\circ}\text{C} = 15(.1646 + .0004 \times 15)1.0 = \underline{2.6}$$

$$\text{Heat required to bring 1 Kgm to } 1000^{\circ}\text{C} = 552.0 \quad "$$

$$55^{\circ} \times .25 \text{ (See Vogt's rule) L.H.F.} = \underline{138.0} \quad "$$

$$\text{Heat required to bring 1 Kgm to } 1000^{\circ}\text{C} = 690.0 \quad "$$

$$\text{Total heat required for 239 Kgm} = 690 \times 239 = 164910.0 \quad "$$

Note:

The foregoing results are slightly higher than those obtained by Akerman on furnace slags, though direct comparison is impossible, as his slags differ somewhat in composition from these.

ZnO.

Heat required to raise 1 Kgm to 1000°C is

$$1000(.0906 \times .000044 \times 1000)1.0 = 134.6 \text{ calories}$$

$$\text{Heat in 1 Kgm at } 15^{\circ}\text{C} = 15(.0906 \times .000044 \times 15) = \underline{1.4} \quad "$$

$$\text{Latent heat of fusion, } 133.2 \quad "$$

$$\begin{aligned} \text{according to Vogt} &= 53.3 \quad " \\ \text{(By 2.1 T rule} &= 30.0 \text{ calories)} \end{aligned}$$

Heat required to bring 1 Kgm to 1000°C = 166.5 calories

Total heat for 335.3 Kgm = $335.3 \times 166.5 = 55827.5$ calories

Al_2O_3

Heat required to bring 1 Kgm to 1000°C is

$1000(0.2081 + 0.00005 \times 1000)1.0 = 259.1$ calories

Sensible heat at 15°C = $15(0.2081 + 0.00005$

$\times 15) \times 1.0 = 4.7$ "

Latent heat of fusion by 2.1 T rule

$\frac{2.1 \times (800 + 273)}{2 \times 27 + 3 \times 16} = 22.1 = 22.1$ "

Total heat required for 72.6 Kgm

$72.6 \times 275.5 = 20001.3$ "

Total heat required then is

Aluminum compounds 200001.3 "

Zinc " 55827.5 "

Fe, bi-silicate 164010.0 "

Mono-silicate 318231.4 "

Sulphide 50528.9 "

Cu Sulphide 110457.5 "

For reduction of Fe_2O_3 to Fe 358710.4 "

For reduction of Fe_2O_3 to FeO 637604.8 "

Total 1726277.8 "

One kilogram of coal, upon burning, gives up 6624 calories. Have 371 Kgm coal burning per hour for four and one-half hours of actual smelting, or 4369 Kgm coal burning while charge is smelting down, and this gives:

$$4369 \times 6624 = 28940256 \text{ calories}$$

Also have heat derived from oxidization of sulphur (See page 21) = 39478.2 calories

and from formation of silicate (See page 21) = 101508.75 calories

Total heat from everything = 29081243 calories

Then efficiency of furnace E is:

$$E = \frac{1726277.2}{29081243.0} = 5.4\% \text{ Efficiency.}$$

Sp gr of matte = 4.8

Ten tons of matte required to be kept in furnace to protect the bottom = 20000#

One cubic foot weighs $4.8 \times 62.5 = 300\#$

Volume of ten tons matte = $\frac{20000}{300} = 67 \text{ cubic feet.}$

The taper with which the furnace widens from the fire bridge to the full width of the laboratory, was increased materially over that at which it tapers in at the flue end. The idea here is to take advantage of the partial vacuum which would be formed, together with the eddy currents, to produce more rapid development of the flame from its cramped condition, as it leaves the grate

and passes over the fire bridge, thus it approaches more nearly the theoretical values calculated for it, and the intense heat which it is capable of developing is realized in the early part of its progress toward the exit flue. This allows a greater temperature rise within the furnace itself, and for a given length of furnace more efficient use of fuel; or in original design mitigates the necessity of extreme lengths.

The fire bridge is of the hollow type, and air is admitted through the bridge into the furnace laboratory, protecting the bridge, and insuring more complete combustion.

The rise of the arch for the first one-half of the furnace length, is one in eight, while at the lower end of the furnace it has diminished to one in twelve. This has been found to give satisfactory results, and is common practice, so is adhered to here.

Two expansion areas are included in both sides and roof of furnace, the details of which are shown in the general drawing. Other dimensions, etc., are shown on general drawing, and are self-explanatory.